



## University of International Business and Economics International Summer School

### MAT 220 Linear Algebra and Differential Equations

**Term:** July 2 – August 2, 2018

**Instructor:** Colin McLarty

**Home Institution:** Case Western Reserve University

**Email:** colin.mclarty@case.edu

**Class Hours:** Monday through Thursday, 120 minutes each day

**Office Hours:** TBD

**Discussion Session:** 2 hours each week

**Total Contact Hours:** 66 contact hours (45 minutes each)

**Credit:** 4 units

#### **Course Description:**

We present core topics in elementary differential equations and related concepts and methods of elementary linear algebra, with emphasis on real-world applications: First-Order and Second Differential Equations; Exact and separable Equations; Mathematical Models and Numerical Methods; Linear Systems and Matrices; Vector Spaces; Higher-Order Linear Differential Equations. The course has a prerequisite of one year of calculus (differential and integral calculus in one variable) and will require use of a laptop computer.

The textbook is supplemented by various course material and video lectures by the author, described at his web page <http://math.mit.edu/~gs/dela/>

#### **Course Goals:**

A student who satisfactorily completes this course will be able to:

- ✧ understand what a differential equation is, especially linear differential equations;
- ✧ understand how differential equations are used to model real life phenomena;
- ✧ relate the theory to graphical and numerical methods of solution;
- ✧ understand the basics of linear algebra;
- ✧ relate linear algebra to techniques for solving linear differential equations.

#### **Required Textbook:**

Gilbert Strang: *Differential Equations and Linear Algebra*, ISBN-10: 0980232791 ISBN-13: 978-0980232790.

#### **Grading Policy:**

Grading will be determined by a combination of class attendance and participation, and the results of your exams. Attendance and Participation 20%. In class short assignments 20%. Midterm Exam, 20%. Final Exam 40%.

### Grading Scale:

Assignments and examinations will be graded according to the following grade scale:

<b>A</b>	90-100	<b>C+</b>	72-74
<b>A-</b>	85-89	<b>C</b>	68-71
<b>B+</b>	82-84	<b>C-</b>	64-67
<b>B</b>	78-81	<b>D</b>	60-63
<b>B-</b>	75-77	<b>F</b>	below 60

### Class Rules:

Students are expected to come to lecture having read the material assigned for the day, and prepared to engage in active discussion about those ideas.

### Attendance Policy:

Summer school is very intense and to be successful, students need to attend every class. Occasionally, due to illness or other unavoidable circumstance, a student may need to miss a class. UIBE policy requires a medical certificate to be excused. Any unexcused absence may affect the student's grade. Moreover, UIBE policy is that a student who has more than 1/3 (6 times) of the class in unexcused absences will fail the course.

### Course Schedule :

#### Week One:

Chapter One.

First order differential equations.

Four examples, linear versus nonlinear, exponentials and sinusoids, the logistic equation, separable and exact equations.

Begin Chapter Two.

Examples of second order equations.

#### Week Two:

Chapter Two.

Second order differential equations.

Constant coefficients, forced oscillations and exponential response.

Electrical network and mechanical systems.

General results on solving second order equations.

Midterm Examination 20%.

#### Week Three:

Chapter Three.

Graphical and numerical solutions.

Nonlinear equations.

Sources, sinks, and saddles.

Linearization and stability.

Basic Euler Methods.

Begin Chapter Four.



**Week Four:**

Chapters Four and parts of Five.

Linear equations and vector spaces.

Solving linear equations by elimination.

Matrix multiplication and inverse.

Column and row space of a matrix, and null-space and image space of a linear transform.

Independence, basis, and dimension.

Introduction to eigenvalues of a matrix.

**Week Five:**

Chapter Six.

Systems of linear differential equations.

Linear systems  $y' = Ay$ .

The exponential of a matrix.

Second order systems.

Final Examination 40%.